

Symbol	Description	Value	Units	Comment
a	acclimation rate	0.3	yr^{-1}	assumed to take about 3 yrs to acclimate
*	Active tissue litter fall	295		Sollins et al. (1980 Fig 2)
a_A	Active biomass turnover rate	0.234126984	yr^{-1}	Claculated from Eq for LC
*	Woody litterfall	475		Sollins et al. (1980 Fig 2)
a_W	Woody biomass turnover rate	0.01123197	yr^{-1}	Claculated from Eq for LC
B_A	Active biomass	1260	g C m^{-2}	Sollins et al. (1980 Table 2)
B_{Amax}	Maximum active biomass	1596.575342	g C m^{-2}	calculated from Eq for BA
B_C	Plant C	43550	g C m^{-2}	Sollins et al. (1980 Table 2)
B_N	Plant N	73.616	g N m^{-2}	Sollins et al. (1980 Table 2)
B_{NF}	BA at canopy closure	630	g C m^{-2}	assumed 1/2 steady state
B_P	Plant P	11.1704	g P m^{-2}	Sollins et al. (1980 Table 2)
B_W	Woody biomass	42290	g C m^{-2}	calculated from Eq for BW
C_a	Atmospheric CO2	386	ppm	http://www.esrl.noaa.gov/gmd/ccgg/trends/
D_C	Detritus and microbe C	19960	g C m^{-2}	Sollins et al. (1980 Table 4)
D_N	Detritus and microbe N	419.5	g N m^{-2}	Sollins et al. (1980 Table 4)
D_P	Detritus and microbe P	41.95	g P m^{-2}	assumed 1/10 of DN; Sollins et al. (1980 Table 4) extractable only
E_N	Inorganic N	2.6	g N m^{-2}	Rastetter et al. (2001 Table 1)
E_P	Inorganic P	0.26	g P m^{-2}	assumed 1/10 of EN
F_{max}	Maximum symbiotic N fixation	0.00135	$\text{g N g}^{-1} \text{C yr}^{-1}$	adjusted to match Cleveland et al. (1999 Table 4b)
F_{NP}	N fixation potential	0	$\text{g N m}^{-2} \text{yr}^{-1}$	calculated from Eq for FNP
G_{mC}	Microbial DC use	1287.5	$\text{g C m}^{-2} \text{yr}^{-1}$	calculated from Eq for GmC
G_{mN}	Microbial DN use	102.6021145	$\text{g N m}^{-2} \text{yr}^{-1}$	calculated from Eq for GmN

G_{mP}	Microbial DP growth	15.00968922	$\text{g P m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for GmP
I_{ND}	N deposition rate	0.2	$\text{g N m}_1^{-2} \text{ yr}^{-1}$	Sollins et al. (1980 Fig 3)
I_{NF}	Non-symbiotic N fixation	0.28	$\text{g N m}_1^{-2} \text{ yr}^{-1}$	Sollins et al. (1980 Fig 3)
I_P	P inputs to inorganic stock	0.05	$\text{g P m}_1^{-2} \text{ yr}^{-1}$	Sollins et al. (1980 Fig 3)
k_C	Plant CO2 half saturation constant	350	ppm	Rastetter et al. (2001)
k_{mN}	Microbial N half saturation constant	0.231	g N m^{-2}	Assumed 1/2 plant value
k_{mP}	Microbial P half saturation constant	0.57	g P m^{-2}	Assumed 1/2 plant value
k_N	Plant N half saturation constant	0.462	g N m^{-2}	Williams and Yanai 1996 assuming 0.45 m3 H2O
k_{NF}	N fix inhibition constant	0.02	$\text{m}^2 \text{ g}^{-1} \text{ C}$	adjusted so symbiotic N fixation peaks ~ year 90
k_P	Plant P half saturation constant	1.14	g P m^{-2}	Williams and Yanai 1996 assuming 0.45 m3 H2O
L_C	Litter C	770	$\text{g C m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for LC
L_N	Litter N	6.505214533	$\text{g N m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for LN
L_P	Litter P	1.240046367	$\text{g P m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for LP
M_N	Gross N mineralization	26.02085813	$\text{g N m}_1^{-2} \text{ yr}^{-1}$	assume 4 x net as implied by 15N data of Nadelhoffer et al. (1999 Fig 1 slope = 0.25)
M_P	Gross P mineralization	2.602085813	$\text{g P m}_1^{-2} \text{ yr}^{-1}$	assumed 1/10 of MN
P_{max}	Maximum Net primary production	1.165227404	$\text{g C m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for Pn

P_n	Net primary production	770	$\text{g C m}^{-2} \text{ yr}^{-1}$	calculated from steady state Eq for BC
q_{mN}	Immobilization C:N ratio	8	$\text{g C g}^{-1} \text{ N}$	Brady (1974: p151)
q_{mP}	Immobilization C:P ratio	56	$\text{g C g}^{-1} \text{ P}$	Assume molar N:P = 16:1
q_N	Plant optimal C:N ratio	591.5833514	$\text{g C g}^{-1} \text{ N}$	calculated from Eq. for q_N
Q_N	Inorganic N leaching	0.0144	$\text{g N m}^{-2} \text{ yr}^{-1}$	3% of total N losses Currie et al (1996 Table 7)
q_{NA}	Active tissue C:N ratio	58.74947545	$\text{g C g}^{-1} \text{ N}$	Sollins et al. (1980 Table 2)
q_{NLA}	Active tissue litter C:N ratio	90.0704357	$\text{g C g}^{-1} \text{ N}$	Sollins et al. (1980 Table 3)
q_{NLW}	Woody tissue litter C:N ratio	147.0588235	$\text{g C g}^{-1} \text{ N}$	Sollins et al. (1980 Table 3)
q_{NW}	Woody tissue C:N ratio	810.6346681	$\text{g C g}^{-1} \text{ N}$	Sollins et al. (1980 Table 2)
Q_{OC}	Organic C leaching	255	$\text{g C m}^{-2} \text{ yr}^{-1}$	calculated from steady state Eq for DC
Q_{ON}	Organic N leaching	0.4656	$\text{g N m}^{-2} \text{ yr}^{-1}$	calculated total inputs minus Q_N
Q_{OP}	Organic P leaching	0.025	$\text{g P m}^{-2} \text{ yr}^{-1}$	calculated total inputs minus Q_P
q_P	Plant optimal C:P ratio	3898.696555	$\text{g C g}^{-1} \text{ P}$	calculated from Eq. for q_P
Q_P	Inorganic P leaching	0.025	$\text{g P m}^{-2} \text{ yr}^{-1}$	assumed 1/2 inputs
q_{PA}	Active tissue C:P ratio	286.1035422	$\text{g C g}^{-1} \text{ P}$	Sollins et al. (1980 Table 2)
q_{PLA}	Active tissue litter C:P ratio	363.0562046	$\text{g C g}^{-1} \text{ P}$	Sollins et al. (1980 Table 3)
q_{PLW}	Woody tissue litter C:P ratio	1111.111111	$\text{g C g}^{-1} \text{ P}$	Sollins et al. (1980 Table 3)
q_{PW}	Woody tissue C:P ratio	6250	$\text{g C g}^{-1} \text{ P}$	Sollins et al. (1980 Table2)
Q_{10Pn}	Q10 NPP	1.4	none	assumed value

Q_{10UN}	Q10 plant N uptake	2	none	assumed value
Q_{10UP}	Q10 plant P uptake	2	none	assumed value
Q_{10Nfix}	Q10 Nfix	2	none	assumed value
Q_{10DC}	Q10 soil C turnover	2	none	assumed value
Q_{10DN}	Q10 soil N turnover	2	none	assumed value
Q_{10DP}	Q10 soil P turnover	2	none	assumed value
Q_{10mUN}	Q10 microbial N uptake	2	none	assumed value
Q_{10mUP}	Q10 microbial P uptake	2	none	assumed value
R_C	Plant C requirement	770	$\text{g C m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for RC
R_m	Microbial respiration	515	$\text{g C m}_1^{-2} \text{ yr}^{-1}$	Sollins et al. (1980 Fig 2)
r_{mC}	microbial DC use	0.064504008	yr^{-1}	calculated from Eq for Rm assuming maximum C efficiency
r_{mN}	microbial DN use	0.244581918	yr^{-1}	calculated from Eq for MN
r_{mP}	microbial DP use	0.357799505	yr^{-1}	calculated from Eq for MP
R_N	Plant N requirement	6.505214533	$\text{g N m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for RN
R_P	Plant P requirement	1.240046367	$\text{g P m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for RP
U_{mC}	Microbial C uptake	772.5	$\text{g C m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for UmC
U_{mN}	Microbial N uptake	19.9812436	$\text{g N m}_1^{-2} \text{ yr}^{-1}$	calculated from steady state Eq for EN
U_{mP}	Microbial P uptake	1.387039446	$\text{g P m}_1^{-2} \text{ yr}^{-1}$	calculated from steady state Eq for EP
U_N	Plant N uptake	6.505214533	$\text{g N m}_1^{-2} \text{ yr}^{-1}$	calculated from steady state Eq for BN
U_{nC}	Net C growth	0	$\text{g C m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for UnC

U_{Nfix}	Symbiotic N fixation	0	$\text{g N m}_1^{-2} \text{ yr}^{-1}$	assumed 0 in mature state
U_{Nmax}	Maximum plant N uptake	0.006080271	$\text{g N g}^{-1} \text{ C yr}^{-1}$	calculated from Eq for UN
U_{nN}	Net N growth	0	$\text{g N m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for UnN
U_{nP}	Net P growth	0	$\text{g P m}_1^{-2} \text{ yr}^{-1}$	calculated from Eq for UnP
U_P	Plant P uptake	1.240046367	$\text{g P m}_1^{-2} \text{ yr}^{-1}$	calculated from steady state Eq for BP
U_{Pmax}	Maximum plant P uptake	0.005299343	$\text{g P g}^{-1} \text{ C yr}^{-1}$	calculated from Eq for UP
V_C	Plant C uptake assets	0.333333333	fraction	assumed 1/3 total
V_N	Plant N uptake assets	0.333333333	fraction	assumed 1/3 total
V_P	Plant P uptake assets	0.333333333	fraction	assumed 1/3 total
α_N	Inorganic N leaching constant	0.005538462	yr^{-1}	calculated from Eq for QN
α_{OC}	Organic C leaching constant	0.012775551	yr^{-2}	calculated from Eq for QOC
α_{ON}	Organic N leaching constant	0.001109893	yr^{-3}	calculated from Eq for QON
α_{OP}	Organic P leaching constant	0.000595948	yr^{-4}	calculated from Eq for QOP
α_P	Inorganic P leaching constant	0.096153846	yr^{-1}	calculated from Eq for QP
β_N	N immobilization rate constant	0.000183269	$\text{g N g}^{-1} \text{ C yr}^{-1}$	calculated from Eq for UmN
β_P	P immobilization rate constant	2.61091E-05	$\text{g P g}^{-1} \text{ C yr}^{-1}$	calculated from Eq for UmP
γ_B	Allometric constant	0.13724278	fraction	Fit to data from Sollins et al. 1980 and Bormann and Sidle 1990
γ_{NF}	Non-symbiotic N fixation constant	0.000230674	$\text{g N m}^{-2/3} \text{ yr}^{-1}$	calculated from Eq for INF

ε_{Cx}	Maximum microbial C efficiency	0.6	fraction	Rastetter et al. (2001)
ε_{mC}	Microbial C efficiency	0.6	fraction	calculated from Eq for ε_{mC}
ε_{mN}	Microbial N efficiency	0.787729276	fraction	calculated from Eq for ε_{mN}
ε_{mP}	Microbial P efficiency	0.841304576	fraction	calculated from Eq for ε_{mP}
η_C	Microbial optimal C asset allocation	1	none	calculated from Eq for h_C
η_N	Microbial optimal N asset allocation	1	none	calculated from Eq for h_N
η_P	Microbial optimal P asset allocation	1	none	calculated from Eq for h_P
ρ_M	Plant multiplicative scaling constant	7.389196499	$\frac{g\ C\ m^2\ yr^2}{g^{-1}\ N\ g^{-1}\ P}$	calculated so $P*n = Pn$
ρ_{mM}	Microbial multiplicative scaling constant	0.000298513	$\frac{m^4\ yr^2\ g^{-1}}{N\ g^{-1}\ P}$	calculated so $G*mC = GmC$
ϕ_N	Growth-increment N:C	0.001329895	$g\ N\ g^{-1}\ C$	calculated from Eq for f_N
ϕ_P	Growth-increment P:C	0.000180342	$g\ P\ g^{-1}\ C$	calculated from Eq for f_P
Ψ	Weighted requirement	1	none	calculated from Eq for Y
Ψ_N	Stoichiometric net N growth	0	$g\ N\ m_1^{-2}\ yr^{-1}$	calculated from Eq for Y_N

Citations:

- Bormann, B.T., and R.C. Sidle. 1990. Changes in productivity and distribution of nutrients in a chronosequence at Glacier Bay National Park, Alaska. *J Ecol* 78:561-578.
- Brady, N.C. 1974. *The Nature and Properties of Soils*, 8th Edition. MacMillan Publishing Co. New York. 639 pp.
- Currie, W.S., J.D. Aber, W.H. McDowell, R.D. Boone, and A.H. Magill. 1996. Vertical transport of dissolved organic C and N under long-term N amendments in pine and hardwood forests. *Biogeochemistry* 35:471-505.
- Nadelhoffer, K.J., B.A. Emmett, P. Gundersen, O.J. Kjønaas, C.J. Koopmans, P. Schleppi, A. Tietema, and R.F. Wright. 1999. Nitrogen deposition makes a minor contribution to carbon sequestration in temperate forests. *Nature* 398:145-148.

- Rastetter, E.B., P.M. Vitousek, C. Field, G.R. Shaver, D. Herbert, G.I. Ågren. 2001. Resource Optimization and Symbiotic N Fixation. *Ecosystems* 4:369-388.
- Sollins, P., C.C. Grier, F.M. McCorison, K. Cromack Jr, R. Fogel, and R.L. Fredricksen. 1980. The internal element cycles of an old-growth Douglas-fir ecosystem in Western Oregon. *Ecol. Monogr.* 50:261-285.
- Willimas, M, and R.D. Yanai. 1996. Multi-dimensional sensitivity analysis and ecological implications of a nutrient uptake model. *Plant and Soil* 180:311-324.